

# A multi-objective approach for improving real-time audio peak reduction and speech clarity in a dental drill noise reduction device

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## Abstract

Audio signals typically comprise several characteristics to be improved by signal processing and in practice, each of these characteristics has a unique relationship to the controllable system parameters. Quantifying these relationships in a multi-objective (MO) approach will enable an improved system setup. This paper determines two novel objective functions of a complex audio signal for the real-time simultaneous improvement of audio peak reduction and speech clarity in a dental drill noise reduction (DDNR) device. The influence of the DDNR system parameters on the outcome of peak reduction and speech clarity is determined by combining response surface methodology and a desirability function to enable MO optimisation. The results show an average improvement of nearly 30% over the original DDNR device performance. The approach described provides an effective means for addressing MO optimisation of other real-time audio signal processing applications where the signal has similar peak reduction and speech clarity objectives to be processed, particularly where the physical outcome is not easy to evaluate in a virtual environment.

## 1 | INTRODUCTION

Audio signals typically comprise several characteristics to be improved simultaneously when being processed by a signal processing algorithm. In practice, each of these characteristics is affected by the algorithm system parameters, requiring a multi-objective (MO) approach. This paper addresses two objectives of an audio signal containing desired speech and undesired dental drill noise, respectively peak reduction and speech clarity. Associated objective functions are then determined for each, which are based on key signal characteristics. This MO approach to peak reduction and speech clarity produces improved results over the original design.

Section 1.1 describes the context of a dental drill noise reduction (DDNR) problem, focusing on the interaction between dental drill noise and speech phenomes to highlight the risk of degrading communication clarity if a broadband noise reduction is employed. A brief description of the DDNR device and the technique it uses for audio signal processing is provided in 1.2. Section 2 describes the theory of how objectives and their associated objective functions are defined in the context of DDNR. Section 3 describes the application of the MO approach, including how to link each objective function to algorithm param-

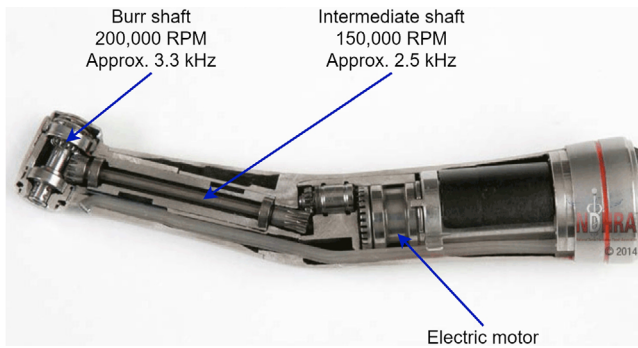
eters. Section 4 discusses the results in terms of the practicality and limitations of the approach and Section 5 concludes the paper.

### 1.1 | Dental drill noise and speech signal

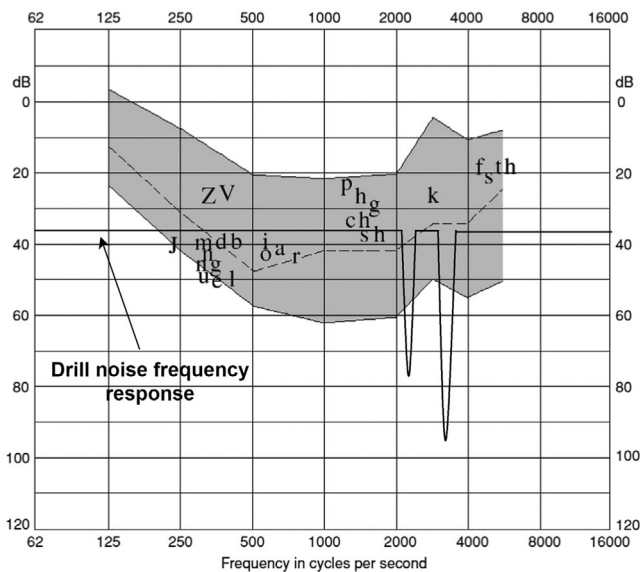
Patient fear of dental drill (also known as a dental handpiece) noise is a worldwide issue [1] that leads to avoidance of treatment, particularly by more extreme sufferers, as well as causing distress to many who still undergo treatment despite their fear. An investigation completed in the UK using the Modified Dental Anxiety Scale (MDAS) [2] suggests that dental drill noise is the most significant cause of patient anxiety, highlighting the need to suppress the noise to improve patient comfort. Noise from a dental drill is generated by its rotating mechanical components. High-speed dental drills are either air turbine-driven or electric motor-driven and their frequencies can vary from 2 to 14 kHz [3]. Figure 1 illustrates a typical electric motor driven dental drill as used in this study. An intermediate shaft is driven by an electric motor normally operating at a speed of 150,000 revolutions per Minute (RPM) and the burr shaft (cutting tool) normally operates at a speed of 200,000 RPM.

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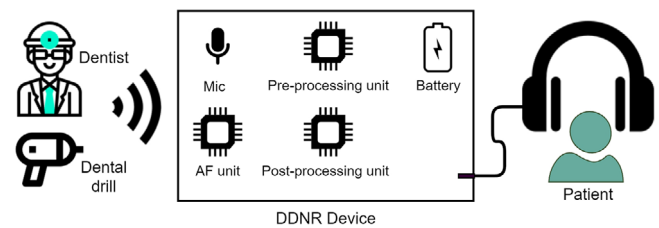
**FIGURE 1** Illustration of a typical electric dental drill (Adapted from Long Star Handpiece [4])



**FIGURE 2** 'Speech banana' frequency audiogram superimposed with a simplified frequency profile of an electric motor driven dental drill at no load (Adapted from Klingpornkun et al [6])

Thus, significant noise peaks due to mechanical resonance are generated at around 2.5 and 3.3 kHz.

In a dentistry environment, verbal communication between dentist and patient is vital to ensure safe and efficient clinical treatment. In an audiogram of sounds from the English language, speech phonemes cluster in a banana shape, which is often referred to as the 'speech banana' [5] as shown in Figure 2. It is broadly used in the assessment of hearing loss [5, 6] but can also indicate the frequency distribution of commonly used speech signals. From this figure, it can be observed that the majority of speech phonemes are within the range of 250 Hz to 5 kHz. Simplified frequency response for an electric motor driven dental drill under no load is also shown in Figure 2. It indicates that the noise to be attenuated, particularly for the two significant noise peaks, is within the frequency spectrum of speech signals. In use, these two drill peaks will reduce their frequencies as the drill comes under load and therefore will interfere with a broader range of speech phonemes than shown.



**FIGURE 3** Schematic illustration of the DDNR device being developed

## 1.2 | The dental drill noise reduction device

Commercial active noise cancelling (ANC) devices are widely available. However, they are optimised for high performance and stability at significantly lower frequencies, for example,  $< 1$  kHz [7], than dental drill noise, which is typically  $> 3$  kHz. There are also sound insulation devices available such as ear defenders and in-the-ear plugs but they aim to attenuate a broad range of frequencies that will impair the essential verbal communication between dentist and patient. Thus, both off-the-shelf ANC headphones and sound insulation devices are unsuitable for the target application, which needs to reduce dental drill noise whilst maintaining speech communication. This justifies the need for a DDNR device, whose schematic arrangement is shown in Figure 3.

The mixed speech and drill noise signal are captured by a microphone embedded in the DDNR device. The signal is then conditioned by a pre-processing unit. The signal then passes to a core adaptive filtering (AF) signal processing unit for noise peak reduction and maintenance of speech. The output signal from the AF unit passes to the post-processing unit, in which the signal can be conditioned again and converted back to analogue for a headphone speaker, and then finally received by a human ear.

The main reason for using AF in the DDNR is because it has been successfully applied in noise cancellation for over five decades and is still very popular due to its low cost and adjustability [8]. AF algorithms share similar underlying principles to adaptive control methods in system control [9]. The overall concept of AF is that noise buried within a signal can be estimated and subtracted to enable the desired signal at the input to be better received at the output. Unlike fixed filters, filtering and subtraction in AF are controlled by an adaptive process to reduce the risk of distorting the desired signal or increasing the output noise [10]. AF has been applied to noise cancellation in headphones and proven to be effective for low frequencies [7] but there has been very little research on AF for high-frequency noise reduction applications. In [11–13], AF methods are applied within the domain of signal processing but target on low-frequency noise ( $< 1$  kHz). The potential of adaptive control algorithms for dealing with complex signals and system responses has been demonstrated, (e.g. [14–16]) but again no high-frequency characteristics of signal/system output were mentioned. An AF system using for reducing dental drill noise solely was proposed by Kaymak et al. [17]. Additional needs of improved system capability in mixed-signal processing

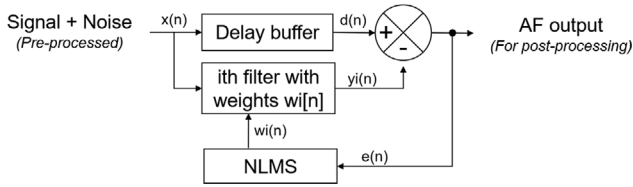


FIGURE 4 Simplified block diagram of the AF algorithm implemented in the DDNR

and maintaining clarity of speech signals have motivated the development of the device investigated here.

The Least Mean Square (LMS) algorithm is the most frequently applied method for noise cancellation due to its simplicity and robustness [18]. Variants of LMS algorithms are widely available, including Normalised LMS (NLMS), which was adopted in the DDNR. NLMS has the advantages of a steadier and faster convergence due to the use of a time-varying step size  $\mu$ . In the DDNR, the NLMS algorithm pre-scales the error to prevent overloading and maintain a more stable LMS. An illustrative block diagram of the NLMS AF algorithm developed for the application is shown in Figure 4.

The AF algorithm applied uses multiple filters, represented by a single block with each filter denoted as the  $i$ th filter in Figure 4. Pre-processed digitalised audio input  $x(n)$  containing the desirable signal (e.g. speech) together with noise (e.g. drill sound) is stored in a delay buffer to synchronise with the filters. In the meantime,  $x(n)$  undergoes processing by one of the filters according to arrays of filter weights  $w_i[n]$ . The filtered output signal  $y_i(n)$  is then subtracted from the delayed signal  $d(n)$  to obtain an error signal  $e(n)$ . Filter weights in each filter are continuously adapted using the NLMS method to minimise  $e(n)$ . Detailed implementation of the AF algorithm is not revealed due to commercial confidentiality and also because the authors do not consider this to be the key purpose of the paper. Besides, whilst AF parameter values are likely to differ in other applications the objective functions and MO approach described here can still be used.

When considering the improvement of filtering performance, there are approaches such as the  $H_\infty$  methods (e.g. [19, 20]) that claim to produce guaranteed high performance and good robustness but they are costly in terms of the mathematical computational power required. In addition, the indirect effect of both unchanged pre- and post-processing units on the resultant noise reduction outcome when the AF parameters change needs to be considered. As a result, the AF algorithm requires careful tuning to incorporate this uncertainty to achieve satisfactory output in the physical domain.

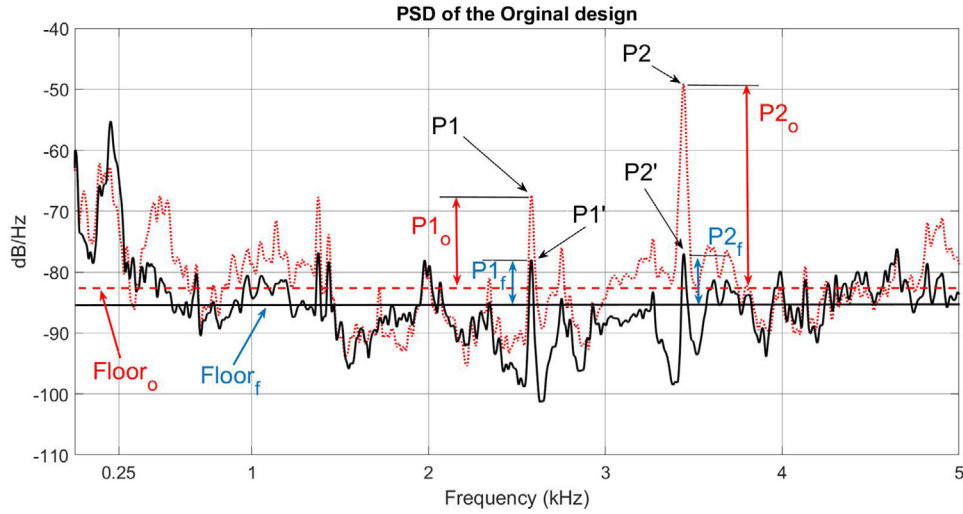
## 2 | OBJECTIVES AND OBJECTIVE FUNCTIONS

Subjective and objective measurements are both commonly applied in the assessment of digitally transmitted speech and audio signal quality [21]. Until the 1990s, subjective mea-

surements by means of human focus groups have been a standard way, which is time-consuming and expensive [22]. Most objective measurement used aims to predict the subjective quality using quantitative models with a focus on speech quality [23]. For example, the perceptual evaluation of speech quality (PESQ) assesses the quality of the output speech signal by comparing with the original input speech signal [24]. Such measures are configured for reducing the effects of background noise (e.g. white and factory noise) [25] that does not have narrow-band high frequency ('peaky') characteristics of drill noise. The primary target of the DDNR device is to eliminate unwanted drill noise peaks, with a secondary target of maintaining effective verbal communication. Therefore, new objective measures of for evaluating DDNR are required and the key characteristics of the processed signal need to be investigated. Frequency domain techniques [12] are applied here as they can analyse the frequency component of a signal individually. Power spectral estimation is used to perform frequency domain analysis of the original and filtered signals. MATLAB signal process toolbox [26] offers a family of spectral analysis methods amongst which Welch's power spectrum density (PSD) [27] is used here. The digitised sound recording is 24-bit audio with a sampling rate of 48 kHz. A window size of 4096 and 2048 overlapped samples are used to produce a PSD plot. An example audio plot for the original design, that is nominal AF parameter setting is shown in Figure 5. Two key objectives are identified suited to the target purpose of the DDNR device, namely peak reduction and speech clarity. A frequency spectrum of 0 to 5 kHz is focused on as this is the region of interest where both drill noise peaks and speech signal co-exist. The original signal is indicated by a red dotted line and the filtered signal is represented by a black solid line.

For the peak reduction objective (objective 1), two significant peaks are observed in the figure, labelled as P1 and P2, whose frequency characteristics correspond to the resonant frequencies (approx. 2.5 and 3.3 kHz) stated in Section 1.1. Rather than taking the absolute summit value for P1 and P2 from the plot, a peak is defined as the difference between its summit value (dB/Hz) and signal floor (dB/Hz). The signal floor value is obtained by taking the mean of the signal power across the range of 0.25 Hz and 5 kHz referring to the 'speech banana' region. For example, in Figure 5 the original peak power for P1 is indicated by  $P1_o$ , and the original peak power for P2 is indicated by  $P2_o$ , with their signal floor denoted as  $Floor_o$ . Similarly, for the filtered peak P1', its power is indicated by  $P1_f$  and power of filtered peak P2' becomes  $P2_f$ , with a new signal floor denoted as  $Floor_f$ .

Using the above rationale, the objective function ObjPi of peak reduction for each peak Pi can be obtained by subtracting the filtered peak power value from the original peak power value, shown as Equation (1), where  $i$  stands for the  $i$ th peak to be suppressed in the PSD plot, for the drill noise shown in Figure 5,  $i$  equals 1 for P1 and 2 for P2. For the speech clarity objective (objective 2) an inverse based on speech signal loss is used as the objective function, defined as the difference between the original signal floor value  $Floor_o$  and filtered signal floor  $Floor_f$ . The mathematical expression for speech clarity, ObjS, is shown



**FIGURE 5** Example PSD plot for the original design, that is nominal setting. The original signal is shown in red dotted line, the filtered signal is shown in black solid line. Signal floor values are shown by horizontal lines

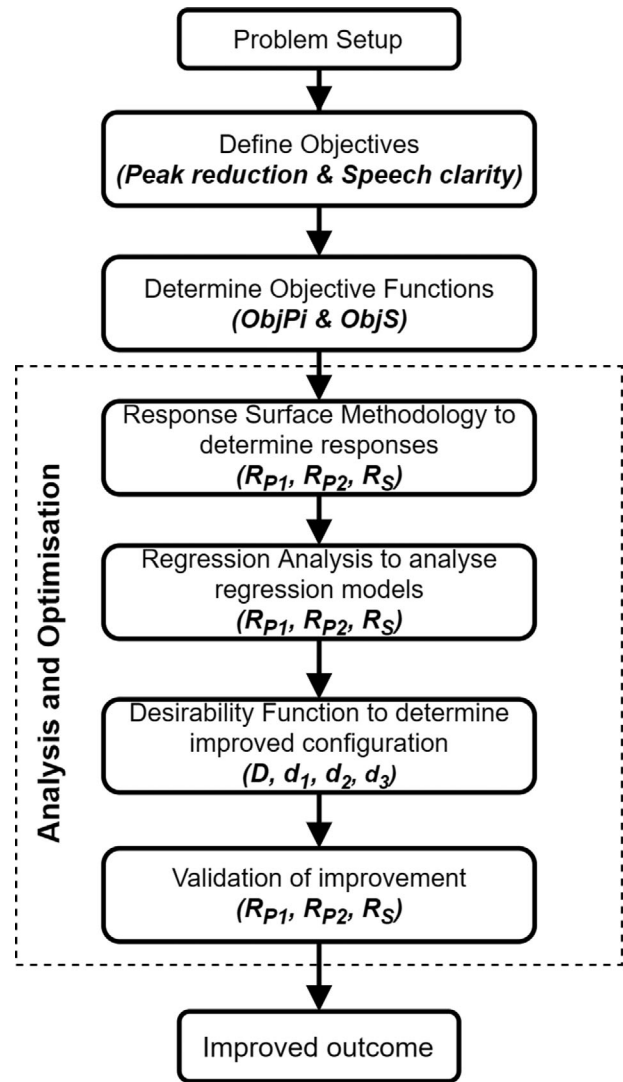
in Equation (2).

$$ObjP_i = P_{i_o} - P_{i_f} = (\text{Power of } P_i - \text{Power of } Floor_o) - (\text{Power of } P_i' - \text{Power of } Floor_f) \quad (1)$$

$$ObjS = \text{Power of } Floor_o - \text{Power of } Floor_f \quad (2)$$

### 3 | MULTI-OBJECTIVE APPROACH

An overview of the MO approach taken for improving real-time audio peak reduction and speech clarity in the DDNR device is shown in Figure 6. With two objectives represented by objective functions (Equations (1) and (2)), the next step is to perform analysis and optimisation starting from the exploration of the influence of AF algorithm parameters. One way of investigating this is through analytical models enabled by computer-based simulation, for example using MATLAB. Analytical models work well when the problem is relatively simple but in real-world scenarios, problems are typically too complex for analytical methods. In this study, the device design is complex and its actual acoustic performance at the headphone output to the ear is the primary interest, making physical experiments more suitable than analytical models. The physical experiments can be kept to a minimum by employing Design of Experiments (DoE), a series of tests in which inputs are varied purposefully to enable observation of their influences on the outcome of a process or system [28]. DoE enables regression models of the objective functions to be obtained and hence predict output responses for given AF parameter values. Response Surface Methodology (RSM) builds on DoE, using statistical techniques to plot surfaces relating responses to several inputs to find an optimum configuration [29]. RSM has broad application in various fields such as chemical [30], biomedical [31] and engineering sciences [32, 33] but RSM for noise cancellation



**FIGURE 6** Overview of the MO approach for improving audio peak reduction and speech clarity



performance improvement is barely addressed in the literature. Despite criticism regarding the time and resources required [34], RSM offers the means of unveiling the complex relationships of the physical situation hence makes it a suitable candidate for this study. In the context of the DDNR device, configurable AF parameters correspond to RSM variables, while the scalar values obtained by applying the objective functions correspond to responses in RSM. For the peak reduction objective, there are two noise peaks P1 and P2 to be attenuated whose response can be obtained by using the same objective function  $\text{ObjP}_i$ , namely  $R_{P1}$  and  $R_{P2}$ . The speech clarity objective,  $\text{ObjS}$ , can be represented by one response namely  $R_S$ . Each of these three responses will have a unique regression model determined by RSM, see Equations (4)–(6). These regression models need to be minimised, maximised or optimised towards a specific target by finding a combination of appropriate variable settings. However, changing the variables will affect all three responses, resulting in a MO optimisation problem to be solved.

The complexity of AF parameter-objective function relationships requires a second-order model to be selected, whose general expression is shown in Equation (3). In the equation, the response is represented by  $y$ ,  $k$  stands for the number of variables,  $i$  and  $j$  are indices of the variables.  $\beta_0$  is the model intercept,  $\beta_i$ ,  $\beta_{ii}$ ,  $\beta_{ij}$  are coefficients corresponding to  $x_i$ ,  $x_i^2$  and  $x_i x_j$  respectively.  $\varepsilon$  represents the model error.

$$y = \beta_0 + \sum_{i=1}^k \beta_i x_i + \sum_{i=1}^k \beta_{ii} x_i^2 + \sum_{i < j}^k \beta_{ij} x_i x_j + \varepsilon \quad (3)$$

Box-Behnken Design (BBD) and Central Composite Design (CCD) are commonly employed RSM methods. CCD can be further categorised into Circumscribed, Inscribed and Faced CCD. Detailed explanations of these methods can be found in [35]. The selection of DoE methods is a case-dependent decision.

Regression Analysis examines the adequacy of the regression models obtained from RSM and decides whether they are suitable for predicting responses with reasonable statistical accuracy. The desirability function approach introduced by Derringer and Suich [36] is adopted for dealing with multiple-objective optimisation due to its successful use in a range of applications such as manufacturing, chemistry and biology [31, 37, 38]. The desirability function first converts system performances (RSM responses) into desirability ratings and uses a single aggregated overall desirability to enable simultaneous optimisation. The desirability function needs to be configured before applying it to the problem. Optimal variable settings for delivering the highest overall desirability rating can then be identified. Validation then needs to be carried out in order to verify the optimisation outcome.

When applying the MO approach, engineering decisions that contribute to a successful outcome need to be made. For example, setup of the experiments should be considered to resemble the actual working environment as close as possible. Therefore, a calibrated GRAS 43AG-1 Ear & Cheek Simulator (ECS) [39] was used to mimic a section of a human head and ear canal for

representing the acoustic characteristics of an actual ear. The ECS contains a GRAS RA0045 externally polarised ear simulator conforming to IEC 60318-4, which works very effectively below 10 kHz [40]. Typical transfer impedance for the RA0045 can be found in [40], which shows that within the frequency range of interest (0 to 5 kHz), the ear simulator is acceptable for this application in evaluating noise reduction of an electric motor driven dental drill. The ECS uses a GRAS 40AG 1/2" externally polarised pressure microphone [41] that conforms to IEC 61094-4. The typical frequency response shows that the microphone is suitable for up to 20 kHz. A GRAS KB0065 Large Right KEMAR Pinna [42] is also used. The ECS is powered by a GRAS 12AD unit, which is also the hardware interface between the ECS and a PC. A high-performance Behringer MS16 16-W monitor speaker was used at a constant volume setting to playback sound recordings representing the sound source. The speaker has a frequency response over the 80 Hz to 20 kHz range [43] that is again suitable for this study. A Windows PC was used to capture the sound data transmitted through the ECS. MATLAB applications were developed to enable data recording and analysis.

The effectiveness of the AF algorithm is assessed by comparing its output with the original combined drill noise and speech signal. Both sounds are transmitted through the DDNR device and its output becomes the signal that is analysed.

The experiment setup for this study is shown in Figure 7, in which a schematic illustration of the device operating environment can be seen in Figure 7(a) and the actual experiment layout can be seen in Figure 7(b). The device is intended to be placed on the patient's chest while they are lying on the treatment chair. An over-the-ear headphone is plugged into the device and will be worn by the patient. An over-the-ear headphone minimises the effect of acoustic transmission from the noise source directly to the ear. Sound will be generated simultaneously during treatment by both the dental drill and the dentist. The nominal distance from the device microphone to the dental drill and the dentist is estimated as 250 mm. The distance from the patient's mouth, where the drill will be located, to the ear is estimated as 100 mm horizontally and 50 mm vertically.

In the implemented AF algorithm (see Figure 4) four adjustable parameters, labelled in brackets, were identified and used as RSM variables. Again, due to commercial confidentiality, only an outline explanation is provided here and these four parameters will be referred to as  $x1$  to  $x4$  from now on. Bearing in mind that these AF parameters are algorithm dependent, which means that different AF methods applied may have different variables to explore.

1. Size of filters ( $x1$ )
2. Size of a delay buffer ( $x2$ )
3. Learning rate for error minimisation ( $x3$ )
4. Filter change rate ( $x4$ )

Initially, the upper and lower limits for these four variables are explored, extending beyond nominal device settings (i.e. the original design of the AF parameters), which equates to  $2^4 = 16$  combinations of variable settings. Preliminary experiments are

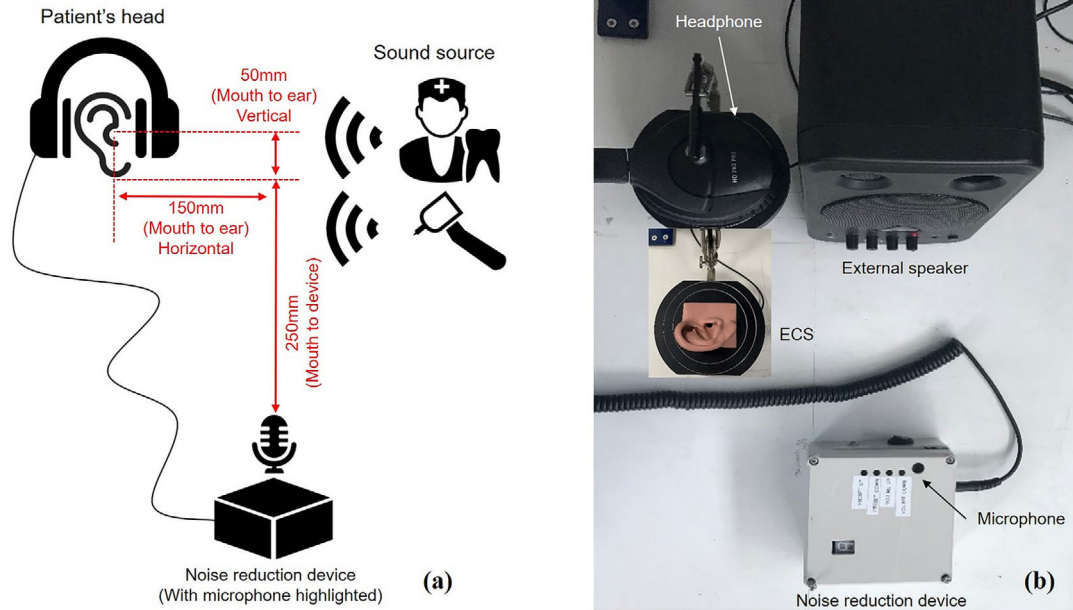


FIGURE 7 Operating environment and experiment setup for improving the DDNR device performance

carried out applying the extreme variable limits to determine the viable design space of AF algorithm parameters. Instability of the algorithm output can be observed from both the MATLAB application and from the hardware LED indicators. When the algorithm output becomes unstable during the preliminary experiments, adjustments are made by either increasing the lower limit or decreasing the upper limit of the variables. When all 16 combinations of variable extremes yield reasonable filtering output then an attainable design space is established.

The lower and upper limits of variables identified in the Planning stage are close to their true limits, therefore using any value outside these ranges poses an unacceptable risk of crashing the system. As a result, inscribed CCD [35] is selected to keep the experimental plan within variable limits and for its capability in modelling quadratic behaviours of responses. A CCD experiment created using MATLAB *ccdesign* function with 4 variables, requires 24 experimental runs plus 12 centre runs (see Appendix 1), which is less than 6% of the equivalent full factorial experiments (625 runs). As each experiment takes approximately 3 min to complete then applying inscribed CCD saves approximately 30 h in total. Codified variables, using  $-1$  for the lower limit and  $+1$  for the upper limit, are used due to commercial confidentiality. The run order is randomised to avoid biased responses. Results collected for each inscribed CCD experiment run can be found in Appendix 1.

MATLAB *fitlm* function [44] is used to fit full quadratic regression models to the results collected for the three responses established in Equations (1) and (2). A summary of the regression analysis can be found at the bottom of Appendix 1 and detailed regression results for each response, including the estimated term coefficients, can be found in Appendix 2. Second-order linear regression models derived from the results

for the three responses are written as Equations (4) to (6).  $R_{P1}$  and  $R_{P2}$  represent the fitted response of objective peak reduction for the first and second noise peak, and  $R_S$  represents the fitted response of objective speech clarity.  $x_1$  to  $x_4$  stand for the four RSM variable identified in the previous section. From Appendix 1 it can be seen that all three regression models are statistically significant given that all p values are significantly less than 0.05. R-squared values for the three models indicate that they are good in terms of explaining the variability in responses, that is representing the empirical relationships between AF parameters and noise reduction performance.

$$\begin{aligned}
 R_{P1} = & 6.74 - 0.6x_1 + 8.9x_2 + 0.45x_3 + 0.28x_4 - 4.78x_1^2 \\
 & - 7.62x_2^2 - 3.7x_3^2 - 0.22x_4^2 - 0.86x_1x_2 + 0.16x_1x_3 \\
 & - 1.01x_1x_4 + 0.07x_2x_3 - 1.51x_2x_4 - 3.33x_3x_4 \quad (4)
 \end{aligned}$$

$$\begin{aligned}
 R_{P2} = & 25 - 3.92x_1 + 3.92x_2 - 0.43x_3 + 0.06x_4 - 6.61x_1^2 \\
 & - 5.62x_2^2 - 0.66x_3^2 + 0.77x_4^2 + 12.22x_1x_2 - 2.09x_1x_3 \\
 & + 0.25x_1x_4 + 0.45x_2x_3 + 1.36x_2x_4 - 0.72x_3x_4 \quad (5)
 \end{aligned}$$

$$\begin{aligned}
 R_S = & 3.61 + 5.49x_1 - 5.33x_2 + 0.31x_3 - 0.14x_4 + 5.06x_1^2 \\
 & + 4.87x_2^2 - 0.41x_3^2 - 0.2x_4^2 - 11.39x_1x_2 + 1.36x_1x_3 \\
 & + 0.09x_1x_4 - 1.72x_2x_3 - 0.32x_2x_4 - 0.14x_3x_4 \quad (6)
 \end{aligned}$$

These regression equations are used to predict responses for the same designs in the designed experiments and then

**TABLE 1** Desirability function types.  $y$  is the response to be optimised,  $L$  is the lower limit,  $U$  is the upper limit,  $T$  is the target,  $r$ ,  $r_1$  and  $r_2$  are the user-specific factors

<b>Larger-the-better (LTB)</b>	$d = \begin{cases} 0, & y < L \\ \left(\frac{y-L}{T-L}\right)^r, & L \leq y \leq T \\ 1, & y > T \end{cases} \quad (7)$
<b>Smaller-the-better (STB)</b>	$d = \begin{cases} 1, & y < T \\ \left(\frac{U-y}{U-T}\right)^r, & T \leq y \leq U \\ 0, & y > U \end{cases} \quad (8)$
<b>Nominal-the-best (NTB)</b>	$d = \begin{cases} 0, & y < L \\ \left(\frac{y-L}{T-L}\right)^{r_1}, & L \leq y \leq T \\ \left(\frac{U-y}{U-T}\right)^{r_2}, & T \leq y \leq U \\ 0, & y > U \end{cases} \quad (9)$

compared with the observed responses for validation. The results are shown in Appendix 3. Columns for variables  $x1$  to  $x4$  are omitted to save space and can be referred to using Appendix 1. A noticeable larger difference is found between predicted and observed responses for  $R_{P1}$  than  $R_{P2}$  and  $R_S$ . A similar conclusion can be drawn from the regression analysis results, in which larger root mean square error, smaller R-squared and adjusted R-squared are obtained. Considering that all three regression models are statistically significant, reflected in their small  $p$  values, plus reasonable R-squared and adjusted R-squared values, then these models were accepted for carrying out the multi-objective optimisation in the next step.

When applying the desirability function response  $y$  to be optimised is converted into an individual desirability  $d$  whose value varies in the range of 0 to 1. If  $y$  reaches its target value then desirability,  $d$ , equals 1, if  $y$  is outside its acceptable range then  $d$  equals 0. Three categories of desirability function are available depending on response target types and are shown in Table 1. Larger-the-better (LTB) means that the response becomes more desirable when its value is large while Smaller-the-better (STB) means that the response should be optimised towards a smaller value. Nominal-the-best (NTB) indicates that there is a specific target value to be achieved for a response, either too large or too small will reduce the desirability.  $d$  represents the desirability rating for the response to be optimised,  $y$  is the quantitative measure of the response.  $L$  is the lower limit of the acceptable range of  $y$ , applicable to LTB and NTB scenarios.  $U$  is the upper limit of the acceptable range of  $y$ , applicable to STB and NTB scenarios.  $T$  is the target value of  $y$ , used in all scenarios.  $r$ ,  $r_1$  and  $r_2$  are user-specified factors ( $> 0$ ). When equals to 1, the desirability function rises linearly from 0 at the bounds to 1 at the target. When set to be larger than 1 this implies that the individual desirability value is relatively small unless the response gets very close to its target value. In other words, the higher the value of  $r$ ,  $r_1$  and  $r_2$  are, the greater the importance of response values being closer to the respective target will be [45]. More detailed explanation and examples of desirability function with different  $r$  values can be found in [46].

When there is more than one response to be optimised, individual desirability ratings  $d_i$  relate to the individual responses  $y_i$  to be optimised. When multi-objective optimisation is required,

**TABLE 2** Desirability functions for three responses  $R_{P1}$ ,  $R_{P2}$  and  $R_S$

Response	Desirability type	$L$	$T$	$U$	$r$
$R_{P1}$	LTB	5	15	N/A	1
$R_{P2}$	LTB	15	30	N/A	1
$R_S$	STB	N/A	0	10	1

Response	Desirability function
$R_{P1}$	$d_1 = \begin{cases} 0, & R_{P1} < 5 \\ \left(\frac{R_{P1}-5}{15-5}\right)^1, & 5 \leq R_{P1} \leq 15 \\ 1, & R_{P1} > 15 \end{cases} \quad (12)$
$R_{P2}$	$d_2 = \begin{cases} 0, & R_{P2} < 15 \\ \left(\frac{R_{P2}-15}{30-15}\right)^1, & 15 \leq R_{P2} \leq 30 \\ 1, & R_{P2} > 30 \end{cases} \quad (13)$
$R_S$	$d_3 = \begin{cases} 1, & R_S < 0 \\ \left(\frac{10-R_S}{10-0}\right)^1, & 0 \leq R_S \leq 10 \\ 0, & R_S > 10 \end{cases} \quad (14)$

that is multiple responses need to be optimised at the same time, an overall desirability  $D$  can be calculated using Equation (10) as a function of  $d_i$  for all the responses to be optimised.  $m$  is the number of responses to be optimised simultaneously and  $i$  is the index of individual responses. Referring to Figure 5 and Equations (1) and (2), objective peak reduction is larger-the-better (LTB), whilst objective speech clarity, which is represented by an inverse measure, is, therefore, smaller-the-better (STB).

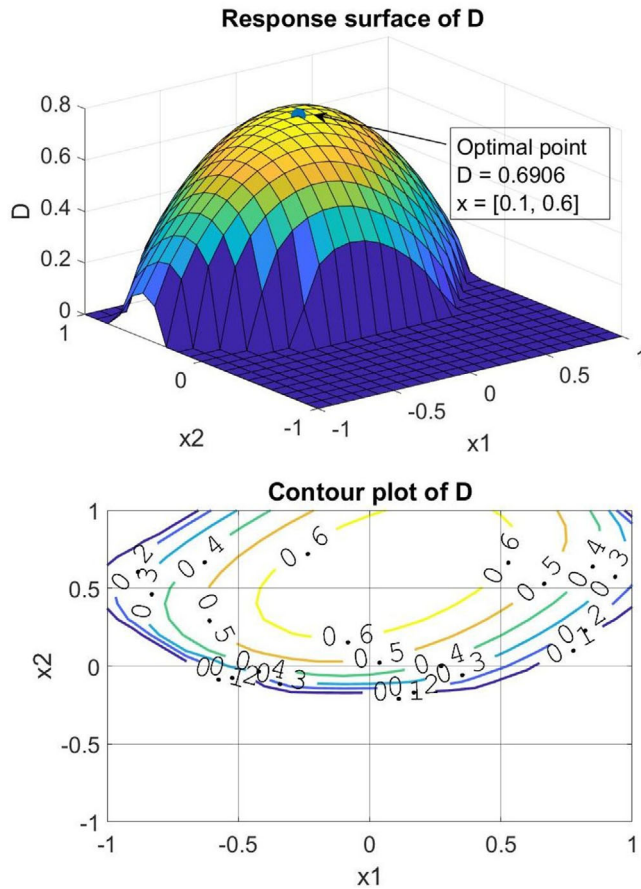
$$D = (d_1 \times d_{i+1} \times \dots \times d_m)^{\frac{1}{m}} \quad (10)$$

The proposed upper ( $U$ ), lower ( $L$ ) and target ( $T$ ) values for the three responses are presented in Table 2. Physical experiments are conducted in order to determine the viable values for these limits. The lower limit for Peak 1 reduction response  $R_{P1}$  is set to be 5 dB/Hz and lower limit for Peak 2 reduction response  $R_{P2}$  is set to be 15 dB/Hz. A 15 dB/Hz target is used for  $R_{P1}$  and 30 dB/Hz target is used for  $R_{P2}$ . For speech clarity response  $R_S$ , an upper limit of 10 dB/Hz is set with its target response set at 0 dB/H. Factor  $r$  is selected to be 1 for all desirability functions, thereby assuming a linear improvement of performance from limits to target values.

After obtaining individual desirability  $d_i$  for each response, the overall desirability  $D$  for all the possible permutations of the four variable settings across the entire design space can be estimated using Equation (10) with  $m$  equal to 3, expressed in Equation (11).

$$D = (d_1 \times d_2 \times d_3)^{\frac{1}{3}} \quad (11)$$

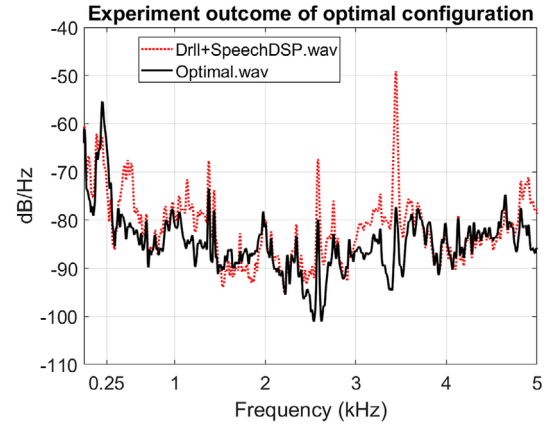
The solution(s) for the  $x1$  to  $x4$  configuration that yields the highest  $D$  value should indicate the optimal setting for the AF algorithm. The largest overall desirability value  $D$  equals 0.6906 is obtained having corresponding variables configured at [ $x1 = 0.1$ ,  $x2 = 0.6$ ,  $x3 = 0.6$ ,  $x4 = -1$ ]. To visualise the results



**FIGURE 8** Response surface and contour plot of overall desirability  $D$  with  $x_3$  and  $x_4$  set at 0.6 and  $-1$  respectively

a 3D response surface and contour plot of  $D$  with respect to  $x_1$  and  $x_2$  are shown in Figure 8, with  $x_3$  set at 0.6 and  $x_4$  set at  $-1$ . In Figure 8, larger  $D$  values indicate better overall desirability and therefore represent better overall noise reduction performance according to the three responses established.

The optimal variable setting  $[0.1, 0.6, 0.6, -1]$  is applied to the AF algorithm to validate the optimisation outcome in the physical domain, with the noise reduction results obtained in the form PSD plot, shown in Figure 9. Details regarding quantified optimised responses are presented in Table 3. Fairly small differences between predicted and observed amongst the three responses suggest the adequacy of the regression models obtained in Equations (4)–(6). The regression model error is indicated by an 11% difference in the overall desirability  $D$  based on comparing experimental results to predicted values. The bottom of Table 3 shows the actual improvement of optimal configurations compared to the original settings in the physical domain. Nominal values of the three responses, that is quantitative performance for the original design shown in the table are obtained by averaging the experiment results for the 12 centre runs in the inscribed CCD. An average of 29.6% improvement for all the three responses is achieved due to optimisation. Significant improvements of 34% and 51% in  $R_{p1}$  and  $R_S$  are also achieved, and a slight improvement of 4% in  $R_{p2}$  is also accomplished.



**FIGURE 9** PSD plot for the optimal design. The original signal is shown in dotted line, the optimised filtered signal is shown in solid line

**TABLE 3** Comparison between tuned AF and original design

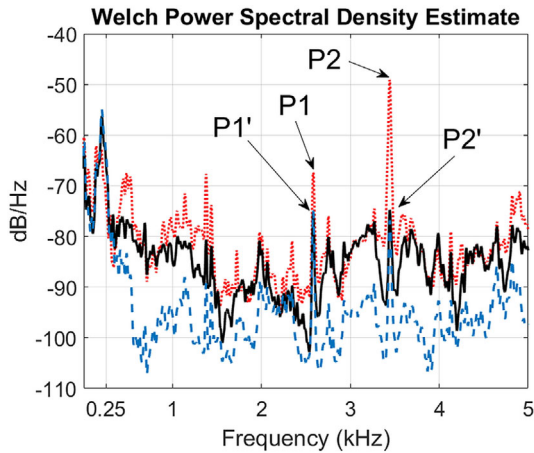
	$R_{p1}$	$R_{p2}$	$R_S$
Predicted response $y$	10.69	25.12	1.53
Observed response $y$	9.01	25.89	1.76
Difference	19%	3%	13%
<b><math>D</math></b>			
Observed overall desirability $D$	0.6906		
Predicted overall desirability $D$	0.6217		
Difference	11%		
	$R_{p1}$	$R_{p2}$	$R_S$
Nominal value of response $y$ (Original design)	6.75	24.97	3.61
Improvement due to optimisation	34%	4%	51%
Average Improvement	29.6%		

## 4 | DISCUSSION

Comparing to previous research on dental drill noise reduction the outcome of this study is encouraging. For example, in [17] an AF algorithm is applied to suppress one air turbine driven dental drill noise peak at 4.2 kHz but with no speech, and in [47, 48] AF is applied to reduce an electric dental drill running at 3.33 kHz again with no speech signals included in the experiment. The simulation results shown in [3] look promising but they are not validated by physical experiments. More importantly, these literature references only deal with a single objective, which is peak reduction. In this work, for example from Table 3, all three responses are optimised with an average improvement of 29.6% as a MO problem. This demonstrates the potential of the approach developed.

When applying this MO approach, identification of objectives and definition of objective functions forms a crucial step.





**FIGURE 10** Comparison of AF outcome for two different configurations. Black dotted line represents the original signal, the black line represents experiment run No. 1 and the blue dashed line represents run No.5

**TABLE 4** Regression statistics comparison between different peak reduction measures

	$R_{P1}$	$R_{P1}^*$	$R_{P2}$	$R_{P2}^*$
RMS error	2.8	2.72	1.44	1.35
$R^2$	0.81	0.749	0.92	0.535
Adjusted $R^2$	0.683	0.582	0.867	0.224
F-test	6.38	4.47	17.3	1.72
$p$ -Value	$8.73e-5$	$1.06e-3$	$1.91e-8$	0.126

Different objective functions will steer the direction of optimisation and hence can lead to distinctly different outcomes. For example, Figure 10 shows the outcome of applying two different AF parameter configurations, corresponding to experiment run No. 1 (black solid line) and 5 (blue dashed line). If a simpler objective function is established that indicates a direct reduction in peak power  $ObjPi^*$  from the original to the filtered signal ( $ObjPi^* = \text{Power of } Pi - \text{Power of } Pi'$ ), then the two modified responses, denoted as  $R_{P1}^*$  and  $R_{P2}^*$ , will yield nearly identical values. This suggests the outcome of objective function  $ObjPi^*$  for objective peak reduction is identical for the two experiments despite the obvious differences observed in the overall signal. This negative effect can be confirmed by performing a regression analysis for  $R_{P1}^*$  and  $R_{P2}^*$ , whose results are shown in Table 4. Noticeably worse regression statistics, for example  $R^2$  and Adjusted  $R^2$  are observed, especially for  $R_{P2}^*$  for which a non-significant model ( $p > 0.05$ ) is obtained. Also, Figure 10 shows using  $ObjPi^*$  instead of  $ObjPi$  does not necessarily represent an actual reduction of the peaks as the relative peak power is still significant compared to signal floor, for example experiment No. 5 (blue dashed line). This means the ‘peaky-ness’ of the filtered signal remains despite the overall power of the signal being reduced. The objective peak reduction defined in this study aims to address the perceived reduction in noise peaks by considering the signal floor. A peak is only being suppressed

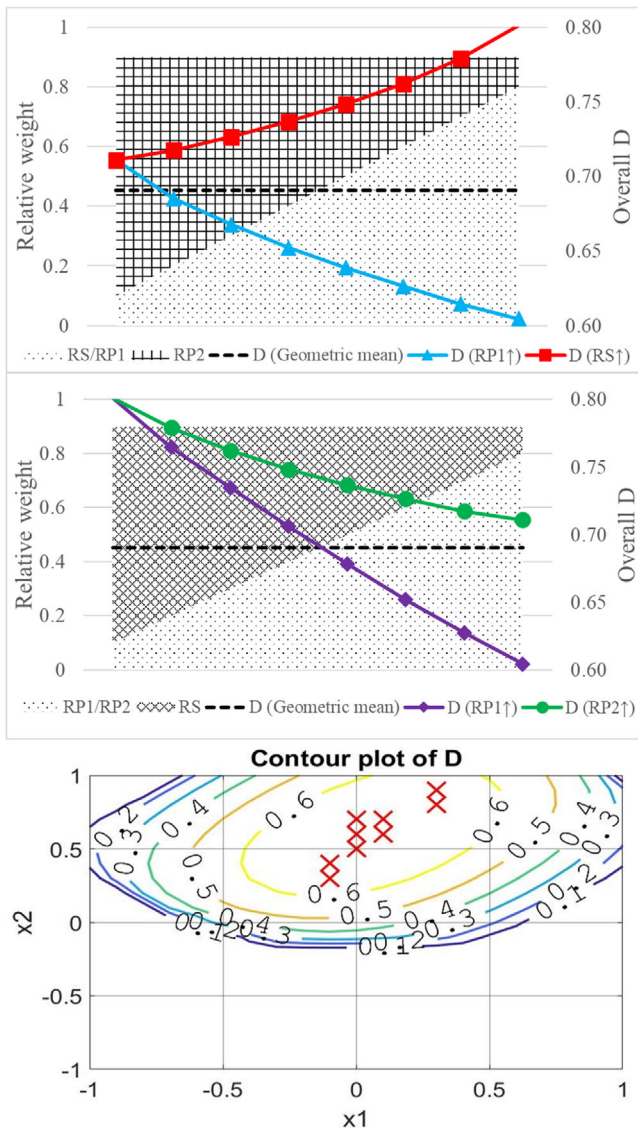
when its relative power to signal floor is reduced, for example experiment run No. 1 (black solid line).

When defining the objective function for objective speech clarity, the initial approach adopted selects specific ‘frequency data points’ from the PSD plot, within the region of interest but away from the two identified noise peaks (2.5 and 3.3 kHz), for example 0.25, 0.5, 0.75, 1, 1.5, 2, 3, 4, 4.5 and 5 kHz to eliminate the effect of signal power difference due to noise peak filtering. This is because the narrowband characteristic of the two peaks is expected to cause a certain effect on the actual differences between signal floors. A comparison of results between applying the ‘frequency data points’ approach described above and the signal floor difference approach used in this study produced a 14% difference in objective function  $ObjS$  values. Different responses  $R_S$  collected for  $ObjS$  could result in different regression equations and hence a different optimal variable configuration. However, in this study, the simplest measure using signal floor difference was effective enough to yield meaningful outcomes. There are situations where signal difference at specific frequencies are of interest then the ‘frequency data point’ approach will offer more practicality.

The use of response desirability is able to aggregate multiple responses into one single measure that is easy to calculate and interpret as found in the literature [37]. The calculations are easily accomplished in MATLAB or similar environments. The formula used for estimating overall desirability  $D$  (see Equation (10)) assumes that all responses are equally important by taking the geometric mean of individual desirability  $d_i$ . This original formulation of overall desirability  $D$  is sufficient in most cases however there are situations where unequal weights are preferred to address the difference in importance for responses [38], an example expression is shown in Equation (15).

$$D = d_1^{w_1} \times d_2^{w_2} \times \dots \times d_i^{w_i} \quad (15)$$

where  $w_i$  indicates the relative importance of each response, with each of them greater than 0 and the sum of them equal to 1, that is  $w_1 + w_2 + \dots + w_i = 1$ . If the relative importance of responses were considered in this study, the outcome of optimisation will be affected. To investigate this a new set of sensitivity analysis varies the relative weights between two responses from 0.1 to 0.8 with a step of change equals to 0.1 while the third response fixed at 0.1. The results are shown in Figure 11. Figure 11(a) illustrates the variation of overall  $D$  when the  $R_{P2}$  weight decreases from 0.8 to 0.1 (indicated by a reducing stacked area) with  $R_S$  or  $R_{P1}$  weight increase from 0.1 to 0.8 (indicated by an increasing stacked area) at the same time. From the figure, It can be seen that when  $R_{P2}$  weight drops  $D$  intends to escalate with the increasing  $R_S$  weight (indicated by red squares) whilst  $D$  intends to drop with the increasing  $R_{P1}$  weight (indicated by blue triangles). Figure 11(b) indicates the variation of overall  $D$  when  $R_S$  weight decreases from 0.8 to 0.1 (indicated by a reducing stacked area) with  $R_{P1}$  or  $R_{P2}$  weight increase from 0.1 to 0.8 (indicated by an increasing stacked area) at the same time. Overall  $D$  drops in both cases when  $R_S$  weight decreases. A more rapid decline of  $D$  is found when  $R_{P1}$  weight increases



**FIGURE 11** Sensitivity analysis of overall desirability  $D$  with regard to different relative weights assigned to the three responses. In (a) and (b) varying responses are represented using different patterns. Overall  $D$  prediction using geometric mean is indicated by a horizontal black dotted line. In (c) all optimal points identified are depicted by red crosses

(indicated by purple diamonds). Figure 11(a) shows that when  $R_{P1}$  weight is set to be 0.1, overall  $D$  stays on top of the value obtained using geometric mean (indicated by a horizontal dotted line), regardless of how relative weight between  $R_S$  and  $R_{P2}$  changes. From Figure 11(a) and Figure 11(b), it is found that the value of overall desirability  $D$  is proportional to the relative weight of response  $R_S$  implying that speech clarity is the easiest to achieve amongst the three responses.  $D$  is more sensitive to  $R_{P1}$  relative weight changes compared to  $R_{P2}$ . Despite the variation observed in overall  $D$  with regard to changing relative weights in the three responses, optimal configurations identified for the system are similar. For example, optimal points for  $x_1$  and  $x_2$  for all situations studied are depicted in Figure 11(c) and superimposed on the contour plot shown in Figure 8. It can be

seen that all points lie within the 0.6 regions of the plot, indicating that varying the relative weights amongst the three response has little effect on the selection of optimal configurations.

The outcome of this sensitivity analysis firstly demonstrates the validity of the desirability function in accomplishing multiple-objective optimisation. This is confirmed by the small variation of the overall  $D$  despite the change in relative weights amongst the three individual desirability ratings. Secondly, in a broader sense, it offers a useful means to investigate the potential effect of response relative weights on the optimal setting of AF parameters.

## 5 | CONCLUSION

Audio signal processing becomes a multi-objective problem when there are several key signal characteristics to be improved at the same time. A MO approach for tackling such problems, using two novel objective functions to define peak reduction and speech clarity, has been presented in this paper and applied to improve the performance of a DDNR device. For the objective of peak reduction, the objective function is established based on the reduction of target noise peak power relative to its signal floor. The objective function for speech clarity is based on a comparison between the original signal floor value and the filtered signal floor value.

The DDNR employs an adaptive filtering (AF) algorithm using the Normalised Least Mean Square (NLMS) method to achieve steady and fast convergence. Exploration of the different empirical relationships between AF parameters and the objectives was enabled by the successful application of response surface methodology (RSM) and the relationships were presented in the form of statistical regression equations. The MO approach described has successfully improved the DDNR performance, in the physical domain, by effectively reducing unwanted noise peaks (peak reduction objective) while keeping the speech signal that is mixed in relatively unaffected (speech clarity objective). The outcome of the MO optimisation is an average overall improvement of nearly 30% compared to the original design, with a 51% specific improvement in objective speech clarity. A next step will be to apply the proposed approach to a more advanced and complex active noise cancelling (ANC) device.

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## REFERENCES

1. Wong, H.M., Mak, C.M., Xu, Y.F.: A four-part setting on examining the anxiety-provoking capacity of the sound of dental equipment. *Noise and Health* 13(55), 385–391 (2011)
2. Humphris, G., et al.: UK population norms for the modified dental anxiety scale with percentile calculator: Adult dental health survey 2009 results. *BMC Oral Health* 13(1), 29, (2013)
3. Khemwong, J., Tangsangumvisai, N.: A two-step adaptive noise cancellation system for dental-drill noise reduction. *Engineering Journal* 22(4), 51–66 (2018)

4. Electric handpiece service. <https://www.lonestarhandpiece.com/electric-handpieceattachment-repair.html> (2019). Accessed October 2019
5. Ross, M.: The Audiogram: Explanation and Significance. Hearing Loss Association of America. Bethesda (2004)
6. Klangpornkun, N., et al.: Predictions from “speech banana” and audiograms: Assessment of hearing deficits in Thai hearing loss patients. *The J. Acoust. Soc. Am.* 134(5), 4132–4132 (2013)
7. Kuo, S.M., Mitra, S., Gan, W.S.: Active noise control system for headphone applications. *IEEE Trans. Control Syst. Technol.* 14(2), 331–335 (2006)
8. Nagal, R., Kumar, P., Bansal, P.: A survey with emphasis on adaptive filter, structure, LMS and NLMS adaptive algorithm for adaptive noise cancellation system. *J. Eng. Sci. Technol. Rev.* 10(2), 150–160 (2017)
9. Zaknich, A.: Principles of Adaptive Filters and Self-Learning Systems - Advanced Textbooks in Control and Signal Processing, 1st ed. Springer London, London (2006)
10. Widrow, B., et al.: Adaptive noise cancelling: principles and applications. *Proc. IEEE* 63(12), 1692–1716 (1975)
11. Sano, H., et al.: Active control system for low-frequency road noise combined with an audio system. *IEEE Transactions on Speech and Audio Processing* 9(7), 755–763 (2001)
12. Souden, M., Benesty, J., Affes, S.: On optimal frequency-domain multi-channel linear filtering for noise reduction. *IEEE Trans. Audio, Speech and Language Processing* 18(2), 260–276 (2010)
13. Seo, M., et al.: Adaptive noise reduction algorithm to improve R peak detection in ECG measured by capacitive ECG sensors. *Sensors* 18(2086), 1–16 (2018)
14. Huo, X., et al.: Event-triggered adaptive fuzzy output feedback control of MIMO switched nonlinear systems with average dwell time. *Appl. Math. Comput.* 365, 124665 (2020)
15. Tokhi, M.O., Hossain, M.A.: A unified adaptive active control mechanism for noise cancellation and vibration suppression. *Mech. Syst. Sig. Process.* 10(6), 667–682 (1996)
16. Ma, L., et al.: Adaptive Fuzzy Tracking Control for a Class of Uncertain Switched Nonlinear Systems with Multiple Constraints: A Small-Gain Approach. *Int. J. Fuzzy Syst.* 21(8), 2609–2624 (2019)
17. Kaymak, E., et al.: Real-time adaptive filtering of dental drill noise using a digital signal processor. In: 7th International Workshop on Research and Education in Mechatronics. pp. 7–11
18. Dixit, S., Nagaria, D.: LMS Adaptive Filters for Noise Cancellation: A Review. *International J. Electr. Comput. Eng. (IJECE)* 7(5), 2520 (2017)
19. Chang, X.H., Yang, G.H.: Nonfragile H filter design for T-S fuzzy systems in standard form. *IEEE Trans. Ind. Electron.* 61(7), 3448–3458 (2014)
20. Li, Z.M., Chang, X.H., Yu, L.: Robust quantized  $H_{\infty}$  filtering for discrete-time uncertain systems with packet dropouts. *Appl. Math. Comput.* 275, 361–371 (2016)
21. Rango, F. De, et al.: Overview on VoIP: Subjective and Objective Measurement Methods. *IJCSNS International Journal of Computer Science and Network Security* 6(1B), 140–153 (2006)
22. Rix, A.W., et al.: Objective assessment of speech and audio quality. *IEEE Trans. Audio, Speech, and Language Processing* 14(6), 1890–1901 (2006)
23. Hu, Y., Loizou, P.C.: Evaluation of objective measures for speech enhancement. In: INTERSPEECH 2006 and 9th International Conference on Spoken Language Processing, INTERSPEECH 2006 - ICSLP (2006)
24. “P.862: Perceptual evaluation of speech quality (PESQ): An objective method for end-to-end speech quality assessment of narrow-band telephone networks and speech codecs”, <http://www.itu.int/rec/T-REC-P.862>. Accessed 23 April 2021
25. Magi, C., et al.: Stabilised weighted linear prediction. *Speech Communication* 51(5), 401–411 (2009)
26. MathWorks: Signal Processing Toolbox. <https://uk.mathworks.com/products/signal.html> (2020). Accessed 1 May 2020
27. Welch, P.D.: The use of fast Fourier transform for the estimation of power spectra: A method based on time averaging over short, modified periodograms. *IEEE Trans. Audio and Electroacoustics*, 15(2), 70–73 (1967)
28. Hinkelmann, K.: Design and Analysis of Experiments, 5th ed. (2012)
29. Myers, R.H.: Response surface methodology - Current status and future directions. *Journal of Quality Technology* 31(1), 30–44 (1999)
30. Vicente, G., et al.: Application of the factorial design of experiments and response surface methodology to optimize biodiesel production. *Ind. Crops Prod.* 8(1), 29–35 (1998)
31. Li, J., et al.: Medium optimization by combination of response surface methodology and desirability function: An application in glutamine production. *Appl. Microbiol. and Biotechnology* 74(3), 563–571 (2007)
32. Palmer, K., Asiabanpour, B., Khoshnevis, B.: Development of a Rapid Prototyping System using Response Surface Methodology. *Qual. Reliab. Eng. Int.* 24(May), 501–502 (2008)
33. Chauhan, S.R., Dass, K.: Optimization of machining parameters in turning of titanium (Grade-5) alloy using response surface methodology. *Mater. Manuf. Processes* 27(5), 531–537 (2012)
34. Arcuri, A., Fraser, G.: Parameter tuning or default values? An empirical investigation in search-based software engineering. *Empirical Software Engineering* 18(3), 594–623 (2013)
35. Myers, R.H., Montgomery, D.C., Anderson-Cook, C.M.: Response Surface Methodology: Process and Product Optimization Using Designed Experiments. Wiley, Hoboken, (2009)
36. Derringer, G., Suich, R.: Simultaneous Optimization of Several Response Variables. *Journal of Quality Technology* 12(4), 214–219 (2013)
37. Lee, D.H., Jeong, I.J., Kim, K.J.: A desirability function method for optimizing mean and variability of multiple responses using a posterior preference articulation approach. *Qual. Reliab. Eng. Int.*, 2018, 34(3), 360–376.
38. Ribardo, C., Allen, T.T.: An alternative desirability function for achieving “six sigma” quality. *Qual. Reliab. Eng. Int.* 19(3), 227–240 (2003)
39. GRAS: GRAS 43AG Ear & Cheek Simulator. <https://www.gras.dk/products/ear-simulator-kit/product/737-43ag> (2020). Accessed 1 May 2020
40. GRAS: Instruction Manual GRAS 60318-4 Ear Simulators’ 2019, p. 21
41. GRAS: GRAS 40AG 1/2" Ext. Polarized Pressure Microphone. <https://www.gras.dk/products/measurement-microphone-cartridge/externally-polarized-cartridges-200-v/product/167-40ag> (2020). Accessed 1 July 2020
42. GRAS: GRAS KB0065 Large Right KEMAR Pinna for 43AG, 45BB and 45BC. <https://www.gras.dk/products/accessories/for-artificial-ears-and-mouths/product/436-kb0065> (2020). Accessed 1 July 2020
43. ‘MS16 - High-Performance, Active 16-Watt Personal Monitor System’, <https://www.behringer.com/product.html?modelCode=P0222>. Accessed 23 April 2021
44. MathWorks: Linear Regression. [https://uk.mathworks.com/help/stats/linear-regression-model-workflow.html?searchHighlight=linearregression&s\\_tid=doc\\_srchtile#btcpwno](https://uk.mathworks.com/help/stats/linear-regression-model-workflow.html?searchHighlight=linearregression&s_tid=doc_srchtile#btcpwno) (2020). Accessed 1 May 2020
45. Costa, N.R., Lourenço, J., Pereira, Z.L.: Desirability function approach: A review and performance evaluation in adverse conditions. *Chemometrics and Intelligent Laboratory Systems* 107(2), 234–244 (2011)
46. Fuller, D., Scherer, W.: Desirability function: Underlying assumptions and application implications. In: Proceedings of the IEEE International Conference on Systems, Man and Cybernetics, pp. 4016–4021
47. Kaymak, E., et al.: Dental drill noise reduction using a combination of Active Noise Control, Passive Noise Control and Adaptive Filtering. In: Inter-Noise 2007, pp. 145–153
48. Kaymak, E., Atherton, M.: Noise Reduction of Dental Drill Noise. In: Mechatronics pp. 1–8

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**APPENDICES**

## Appendix 1 Experiment and regression analysis results applying inscribed CCD

Run order	x1	x2	x3	x4	R <sub>p1</sub>	R <sub>p2</sub>	R <sub>s</sub>
1	-1	0	0	0	4.55	22.35	3.36
2	0	0	0	0	8.78	24.24	4.02
3	0	0	0	0	6.69	23.98	3.87
4	0	0	0	0	8.45	23.35	4.15
5	0	-1	0	0	-6.09	14.07	13.64
6	-0.5	-0.5	0.5	0.5	-2.20	24.90	3.23
7	-0.5	0.5	-0.5	-0.5	8.76	23.33	3.78
8	0.5	-0.5	-0.5	0.5	0.50	16.79	13.26
9	0	0	0	0	7.38	24.98	4.17
10	0.5	-0.5	-0.5	-0.5	-2.24	16.64	12.81
11	0	0	0	0	8.11	24.47	3.54
12	-0.5	0.5	0.5	-0.5	9.30	21.65	2.92
13	0	0	0	0	6.56	23.07	3.30
14	0.5	-0.5	0.5	0.5	-4.48	12.41	15.42
15	-0.5	0.5	-0.5	0.5	10.27	21.82	3.36
16	-0.5	0.5	0.5	0.5	5.94	22.76	2.90
17	0	0	0	1	7.00	25.87	3.41
18	0.5	0.5	0.5	0.5	8.01	25.22	2.86
19	0.5	0.5	-0.5	-0.5	8.80	24.18	3.25
20	0	0	0	0	6.84	26.92	3.12
21	0	0	0	-1	3.88	26.17	3.70
22	0	1	0	0	2.22	25.00	3.53
23	0	0	0	0	6.26	27.65	3.21
24	0.5	-0.5	0.5	-0.5	-0.88	15.20	15.49
25	0	0	0	0	6.23	24.32	3.73
26	0	0	0	0	5.75	25.67	3.35
27	0.5	0.5	-0.5	0.5	9.64	25.34	2.89
28	0	0	-1	0	-0.85	24.21	3.44
29	-0.5	-0.5	-0.5	0.5	-3.59	26.36	2.64
30	-0.5	-0.5	-0.5	-0.5	-3.69	23.83	3.03
31	1	0	0	0	-2.73	14.75	14.19
32	0	0	0	0	5.89	25.57	3.12
33	0	0	0	0	4.02	25.38	3.63
34	-0.5	-0.5	1	-1	-4.06	27.51	2.86
35	0	0	1	0	4.78	24.97	3.24
36	0.5	0.5	1	-1	10.13	22.94	2.91

**Regression analysis**

	R <sub>p1</sub>	R <sub>p2</sub>	R <sub>s</sub>
Error degrees of freedom	21	21	21
Root mean squared error	2.8	1.44	0.397
R-squared	0.81	0.92	0.994
Adjusted R-squared	0.683	0.867	0.991
F-test	6.38	17.3	267
p value	8.73e-5	1.91e-8	2.13e-20



Appendix 2 Regression results for the three responses with coefficients for each term outlined in red

Estimated Coefficients:					Estimated Coefficients:					Estimated Coefficients:				
<b>R<sub>p1</sub></b>	Estimate	SE	tStat	pValue	<b>R<sub>p2</sub></b>	Estimate	SE	tStat	pValue	<b>R<sub>s</sub></b>	Estimate	SE	tStat	pValue
(Intercept)	6.7374	0.78812	8.5487	2.7978e-08	(Intercept)	24.995	0.40601	61.562	3.3062e-25	(Intercept)	3.6149	0.1118	32.333	2.1362e-19
x1	-0.59599	1.1515	-0.51756	0.61018	x1	-3.9155	0.59323	-6.6003	1.5516e-06	x1	5.4902	0.16336	33.609	9.6181e-20
x2	8.8955	1.1515	7.7248	1.4368e-07	x2	3.9243	0.59323	6.6151	1.5021e-06	x2	-5.3363	0.16336	-32.666	1.7292e-19
x3	0.4472	1.1247	0.39761	0.69493	x3	-0.43011	0.57941	-0.74233	0.46611	x3	0.31169	0.15955	1.9535	0.064207
x4	0.2847	1.1247	0.25313	0.80263	x4	0.060347	0.57941	0.10415	0.91804	x4	-0.13692	0.15955	-0.85816	0.40049
x1^2	-4.78	1.9817	-2.4121	0.025095	x1^2	-6.6121	1.0209	-6.4768	2.0358e-06	x1^2	5.0586	0.28112	17.994	3.0697e-14
x2^2	-7.6195	1.9817	-3.8449	0.00094081	x2^2	-5.6216	1.0209	-5.5065	1.8316e-05	x2^2	4.868	0.28112	17.316	6.5482e-14
x3^2	-3.6979	1.8566	-1.9918	0.059557	x3^2	-0.65649	0.95644	-0.68639	0.49998	x3^2	-0.41281	0.26337	-1.5674	0.13196
x4^2	-0.21949	1.8566	-0.11822	0.90701	x4^2	0.77196	0.95644	0.80712	0.42864	x4^2	-0.20126	0.26337	-0.76417	0.45326
x1:x2	-0.85884	2.9007	-0.29608	0.77008	x1:x2	12.224	1.4943	8.1799	5.7553e-08	x1:x2	-11.39	0.41149	-27.68	5.1956e-18
x1:x3	0.15685	2.5837	0.060709	0.95216	x1:x3	-2.0911	1.331	-1.5711	0.13111	x1:x3	1.3628	0.36651	3.7183	0.0012716
x1:x4	-1.0083	2.5837	-0.39026	0.70027	x1:x4	0.24463	1.331	0.18379	0.85594	x1:x4	0.088647	0.36651	0.24187	0.81123
x2:x3	0.070802	2.5837	0.027404	0.9784	x2:x3	0.44787	1.331	0.33649	0.73984	x2:x3	-1.7161	0.36651	-4.6824	0.00012729
x2:x4	-1.5059	2.5837	-0.58284	0.56621	x2:x4	1.3621	1.331	1.0234	0.31778	x2:x4	-0.3188	0.36651	-0.86983	0.39423
x3:x4	-3.3301	2.204	-1.5109	0.14571	x3:x4	-0.71961	1.1354	-0.63378	0.53307	x3:x4	0.14252	0.31266	0.45584	0.65318

Number of observations: 36, Error degrees of freedom: 21 Root Mean Squared Error: 2.8 R-squared: 0.81, Adjusted R-Squared: 0.683 F-statistic vs. constant model: 6.38, p-value = 8.73e-05	Number of observations: 36, Error degrees of freedom: 21 Root Mean Squared Error: 1.44 R-squared: 0.92, Adjusted R-Squared: 0.867 F-statistic vs. constant model: 17.3, p-value = 1.91e-08	Number of observations: 36, Error degrees of freedom: 21 Root Mean Squared Error: 0.397 R-squared: 0.994, Adjusted R-Squared: 0.991 F-statistic vs. constant model: 267, p-value = 2.13e-20
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## Appendix 3 Comparison between predicted and observed results

Run	Observed			Predicted			Difference		
	$R_{P1}$	$R_{P2}$	$R_S$	$R_{P1}$	$R_{P2}$	$R_S$	$R_{P1}$	$R_{P2}$	$R_S$
1	4.55	22.35	3.36	2.55	22.30	3.18	44%	0%	5%
2	8.78	24.24	4.02	6.74	24.99	3.61	23%	3%	10%
3	6.69	23.98	3.87	6.74	24.99	3.61	1%	4%	6%
4	8.45	23.35	4.15	6.74	24.99	3.61	20%	7%	13%
5	-6.09	14.07	13.64	-9.78	15.45	13.82	61%	10%	1%
6	-2.20	24.90	3.23	-1.60	24.66	3.29	27%	1%	2%
7	8.76	23.33	3.78	6.57	21.92	4.20	25%	6%	11%
8	0.50	16.79	13.26	-1.02	15.77	13.28	303%	6%	0%
9	7.38	24.98	4.17	6.74	24.99	3.61	9%	0%	13%
10	-2.24	16.64	12.81	-3.22	15.91	13.28	44%	4%	4%
11	8.11	24.47	3.54	6.74	24.99	3.61	17%	2%	2%
12	9.30	21.65	2.92	8.64	23.12	2.90	7%	7%	1%
13	6.56	23.07	3.30	6.74	24.99	3.61	3%	8%	9%
14	-4.48	12.41	15.42	-2.19	13.71	15.20	51%	10%	1%
15	10.27	21.82	3.36	8.27	22.90	3.79	19%	5%	13%
16	5.94	22.76	2.90	7.01	23.38	2.63	18%	3%	9%
17	7.00	25.87	3.41	6.80	25.83	3.28	3%	0%	4%
18	8.01	25.22	2.86	5.55	24.65	3.15	31%	2%	10%
19	8.80	24.18	3.25	5.97	25.04	3.27	32%	4%	1%
20	6.84	26.92	3.12	6.74	24.99	3.61	1%	7%	16%
21	3.88	26.17	3.70	6.23	25.71	3.55	60%	2%	4%
22	2.22	25.00	3.53	8.01	23.30	3.15	260%	7%	11%
23	6.26	27.65	3.21	6.74	24.99	3.61	8%	10%	12%
24	-0.88	15.20	15.49	-1.06	14.57	15.06	21%	4%	3%
25	6.23	24.32	3.73	6.74	24.99	3.61	8%	3%	3%
26	5.75	25.67	3.35	6.74	24.99	3.61	17%	3%	8%
27	9.64	25.34	2.89	6.66	26.26	2.94	31%	4%	2%
28	-0.85	24.21	3.44	2.59	24.77	2.89	404%	2%	16%
29	-3.59	26.36	2.64	-0.27	24.63	2.73	92%	7%	3%
30	-3.69	23.83	3.03	-3.48	25.01	2.82	6%	5%	7%
31	-2.73	14.75	14.19	1.36	14.47	14.16	150%	2%	0%
32	5.89	25.57	3.12	6.74	24.99	3.61	14%	2%	16%
33	4.02	25.38	3.63	6.74	24.99	3.61	68%	2%	0%
34	-4.06	27.51	2.86	-2.52	26.96	2.93	38%	2%	2%
35	4.78	24.97	3.24	3.49	23.91	3.51	27%	4%	9%
36	10.13	22.94	2.91	8.52	23.72	2.96	16%	3%	2%